

# Angles in Quadrilaterals

## ACMMG202

7 8 9 10 11 12



TI-Nspire



Navigator



Student



50 min

## Objective

Establish properties of quadrilaterals using congruent triangles and angle properties, and solve related numerical problems using reasoning.

## Equipment

For this activity you will need:

- TI-Nspire
- TI-Nspire file: “Angles in Quadrilaterals” (tns)
- TI-Navigator system (Optional)

## Problem 1 – Properties of Rhombi

You will begin this activity by looking at angle properties of rhombi. On page 1.3, you are given rhombus *READ* and the measure of angles *R*, *E*, *A*, and *D*.

### Question: 1.

Move point *E* to four different positions and collect the measures of *R*, *E*, *A*, and *D* and record your measurements in the table below.

| Position | <i>R</i> | <i>E</i> | <i>A</i> | <i>D</i> |
|----------|----------|----------|----------|----------|
| 1        |          |          |          |          |
| 2        |          |          |          |          |
| 3        |          |          |          |          |
| 4        |          |          |          |          |

### Question: 2.

Consecutive angles of a rhombus are \_\_\_\_\_.

### Question: 3.

Opposite angles of a rhombus are \_\_\_\_\_.

Next, you will look at the properties of the angles created by the diagonals of a rhombi. On page 1.7, you are given rhombus *CARD* and the measure of angles *CSA*, *ASR*, *RSD*, and *DSC*.

**Question: 4.**

Move point *C* to four different positions. Angles formed by the intersection of the two diagonals of a rhombus are \_\_\_\_\_.

On page 1.10, you are given rhombus *RHOM* and the measure of all angles created by the diagonals of the rhombus.

**Question: 5.**

The diagonals of a rhombus **bisect** the vertices.

**Problem 2 – Properties of Kites**

You will begin this problem by looking at angle properties of kites. You are given kite *KING* and the measure of angles *K*, *I*, *N*, and *G*.

**Question: 6.**

Move point *I* to two different positions and point *K* to two different positions and collect the measures of *K*, *I*, *N*, and *G* and record your measurements in the table below.

| Position | <i>K</i> | <i>I</i> | <i>N</i> | <i>G</i> |
|----------|----------|----------|----------|----------|
| 1        |          |          |          |          |
| 2        |          |          |          |          |
| 3        |          |          |          |          |
| 4        |          |          |          |          |

**Question: 7.**

What do you notice about the opposite angles of a kite?

Next, you will look at the properties of the angles created by the diagonals of a kite. On page 2.5, you are given kite *BLUE* and the measure of angles *BSL*, *LSU*, *USE*, and *ESB*.

**Question: 8.**

Move point *L* to four different positions. Angles formed by the intersection of the two diagonals of a kite are \_\_\_\_\_.

On page 2.8, you are given rhombi *KITE* and the measure of all angles created by the diagonals of the rhombus.

**Question: 9.**

Move point *K* to four different positions. What do you notice about the angles created by the diagonals of a kite?

### Problem 3 – Properties of Trapezoids

In this problem, you will look at angle properties of trapezoids. You are given trapezoid  $TRAP$  and the measure of angles  $T$ ,  $R$ ,  $A$ , and  $P$ .

**Question: 10.**

Move point  $R$  to four different positions and collect the measures of  $T$ ,  $R$ ,  $A$ , and  $P$  onto the table below.

| Position | $T$ | $R$ | $A$ | $P$ |
|----------|-----|-----|-----|-----|
| 1        |     |     |     |     |
| 2        |     |     |     |     |
| 3        |     |     |     |     |
| 4        |     |     |     |     |

**Question: 11.**

What do you notice about the angles of a trapezoid?

### Problem 4 – Beyond Observation (Extension)

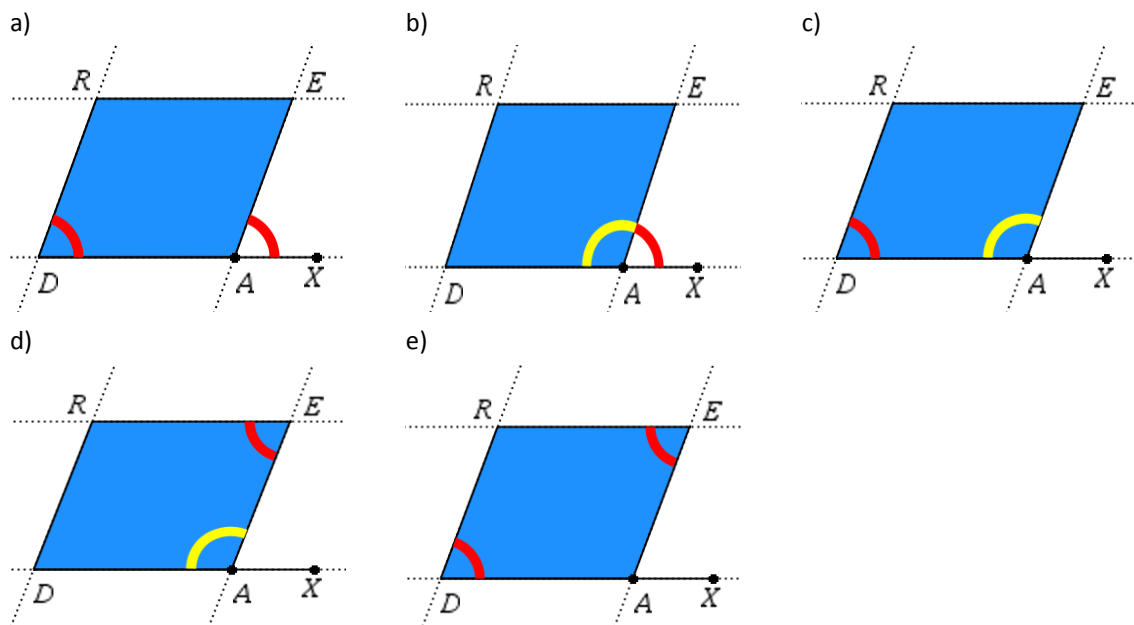
Parallelogram:

“A quadrilateral with pairs of opposite sides parallel”.

Parallelograms have many properties that are a consequence of this definition. In problem 4 a parallelogram has been constructed. On page 4.1 the angle properties are explored through a series of steps. Follow these steps then answer the questions below.

**Question: 12.**

Name and describe the relationship between each angle pair.



The interactive diagram on page 4.2 provides guided steps, to help prove that opposite sides of a parallelogram are equal in length.

**Question: 13.**

Use the interactive diagram to help formulate a proof to show that the opposite sides of a parallelogram are equal.